

Obsen. support for
Hot Big-Bang scenario

(4)

- Hubble expansion

$$H(t) \Big|_{t=t_0} = \frac{\dot{a}(t)}{a(t)} \Big|_{t=t_0} \equiv H_0 > 0$$

- Element abundance

Hydrogen	75%	primordial nucleosynthesis
Helium	24%	
Other	1%	

- Cosmic microwave
background (CMB)

photons once in thermal
equilibrium with charges further
decoupled and formed thermal
background radiation of $T = 2.7^\circ\text{K}$
(blackbody)

- Imprint of information
in CMB

$$\frac{\delta T}{T} \sim \frac{\delta \rho}{\rho} \sim 10^{-5}$$

temperature fluctuations density fluctuations

spherical harmonics
decomposition

$$\frac{\delta T}{T} = \sum_{l,m} a_{lm} Y_{lm}(\theta, \phi)$$

power spectrum
of fluctuations

$$C_l = \langle |a_{lm}|^2 \rangle$$

peak
structure
related to angular
scale in the sky

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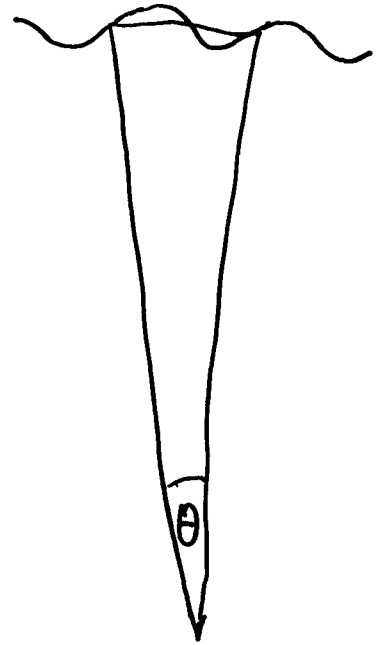
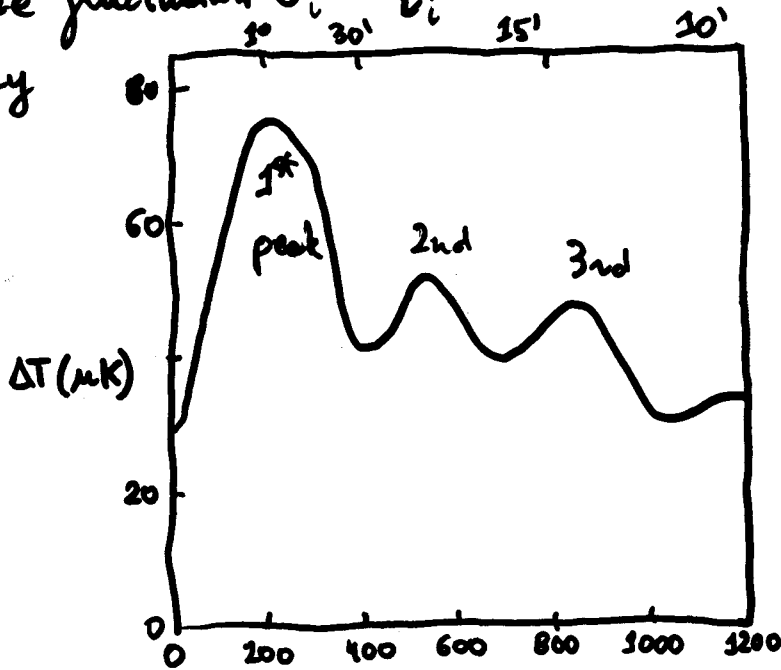
power spectrum
of fluctuations

$$C_l = \langle |a_{lm}|^2 \rangle$$

peak structure
related to angular
scale in the sky

the angle
we can see fluctuation
in the sky
today

$$\theta_i = \frac{\pi}{l_i}$$



peaks give hints about cosmological parameters (k, Ω, Λ)

density parameter

$$\Omega = \sum_i \frac{\rho_i}{\rho_{crit}} \quad \rho_{crit} = \frac{3H^2}{8\pi G}$$

$$\Omega = \underbrace{\Omega_m}_{\downarrow \text{matter}} + \underbrace{\Omega_r}_{\downarrow \text{radiation etc.}} + \Omega_\Lambda + \Omega_d + \dots = 1 + \frac{k}{a^2 H^2}$$

1st peak gives strong
evidence for $\Omega = 1$

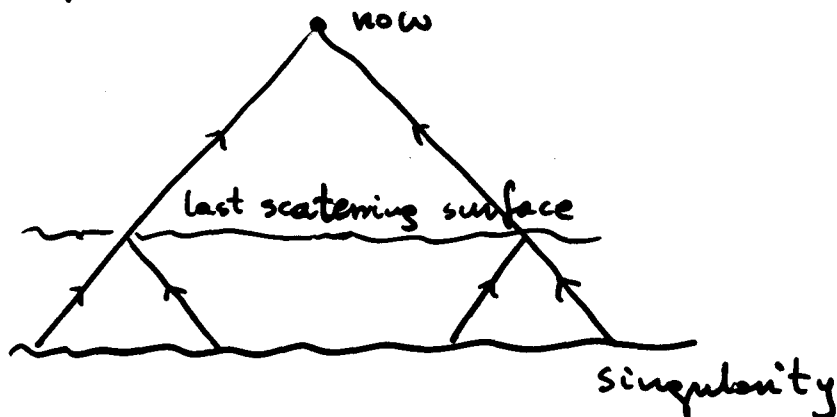
(flat universe)
($k=0$)

THE PUZZLES

of Hot Big-Bang

1. the problem of singularity $t=0$ (people assumed $t \geq 0$ only)
(what was before?)

2. the horizon problem



CMB radiation isotropic ($\frac{\delta T}{T} \sim 10^{-5}$)

though it was not in causal contact

3. the origin of anisotropies of CMB which could give observed structures in the universe

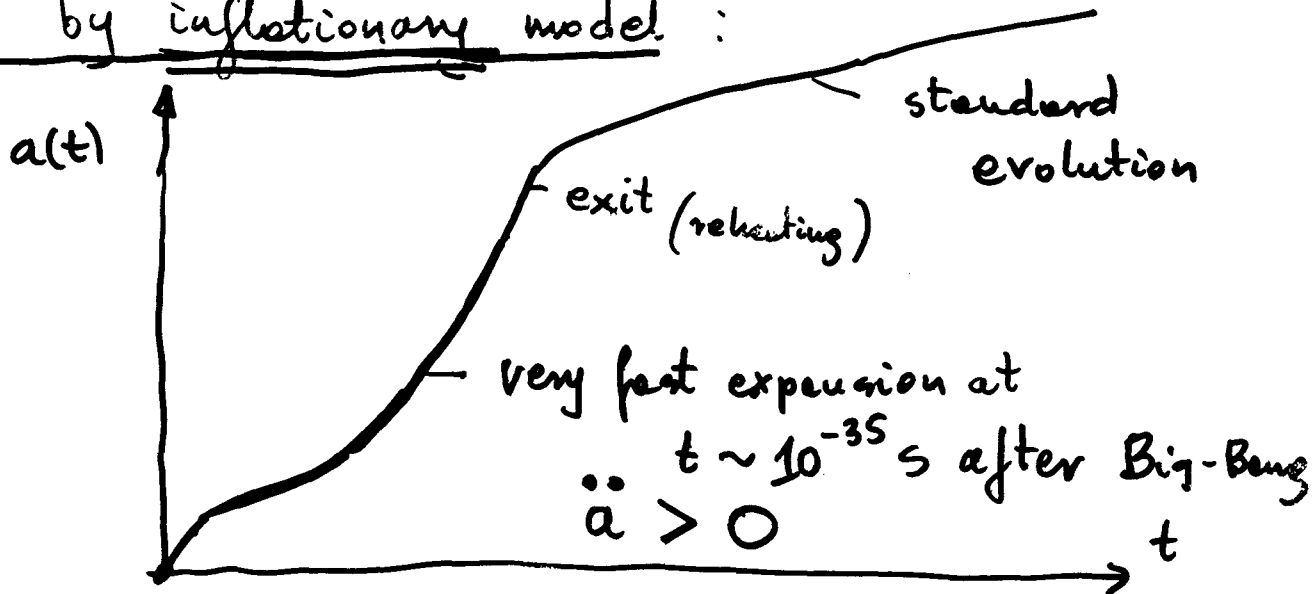
4. flatness problem

strong evidence for $\Omega \approx 1$ — evolving to the past (\sim singularity) $\Omega = 1$

at the very high precision

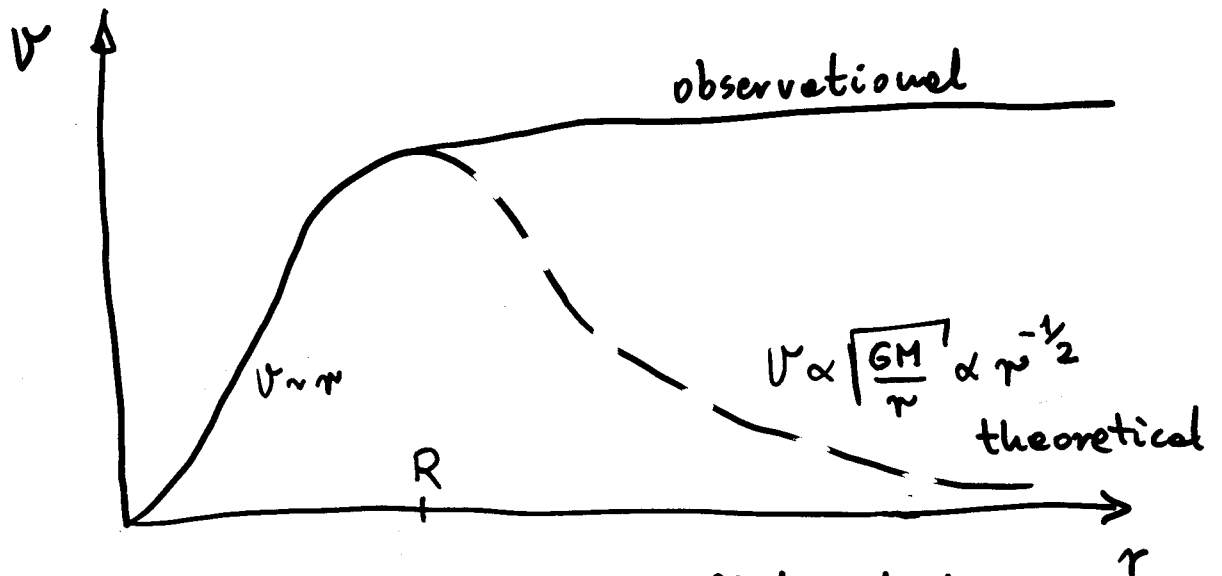
problems 2-4

Solved by inflationary model:



5. dark matter problem

(7)



Galaxies rotation curves flat outside

⇒ there must be some matter which is not visible - dark matter

6. dark energy problem

2nd Einstein equation

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\rho + 3p)$$

accelerated expansion/inflation requires

$$p < -\frac{1}{3}\rho$$

a scalar field potential energy for example

Pressure must be negative!

Deceleration parameter

$$q = -\frac{\ddot{a}a}{\dot{a}^2} < 0$$

This does not seem to be a problem since it refers to the early universe $t \sim 10^{-35}$ s.

Supernovae Ia "revolution" (as standard "candles") (8)

A redshift-magnitude test (generalized Hubble evolution law)

observed

magnitude \rightarrow

$$m(z) = M(z) + 25 + 25 \log cz - 5 \log_{10} H_0 + 1.086 (1 - q_0) z + O(z^2)$$

\swarrow absolute magnitude \downarrow redshift

for nearby galaxies ($z \ll 1$) - Hubble law

$$D = \frac{cz}{H_0}$$

does not include q_0 - not enough

Strong evidence that

$$q_0 < 0$$

or

$$\ddot{a} > 0$$

or

$$p < -\frac{1}{3} \dot{\rho}$$

at the current moment of evolution 0

At least 70% of matter in the universe has negative pressure now - dark energy.

What is the source of dark energy?

cosmological constant Λ ? $p = -\Lambda$

a scalar field / scalar fields

$$\rho = \frac{1}{2} \dot{\phi}^2 + V(\phi)$$

$$p = \frac{1}{2} \dot{\phi}^2 - V(\phi) \quad ?$$

$\leftarrow \dot{\phi} \approx 0$

$$p = -\rho = -\Lambda$$

$V(\phi) \approx 0 \rightarrow$

$$p = \rho$$

more puzzle

$\rho + p < 0$ (phantom requires negative kinetic energy, for example)

$$\rho = -\frac{1}{2} \dot{\phi}^2 + V(\phi)$$

$$p = -\frac{1}{2} \dot{\phi}^2 - V(\phi)$$

tuning other cosm. parameters
requires more sophisticated

$$\phi = \phi(t)$$

and $V = V(\phi(t))$

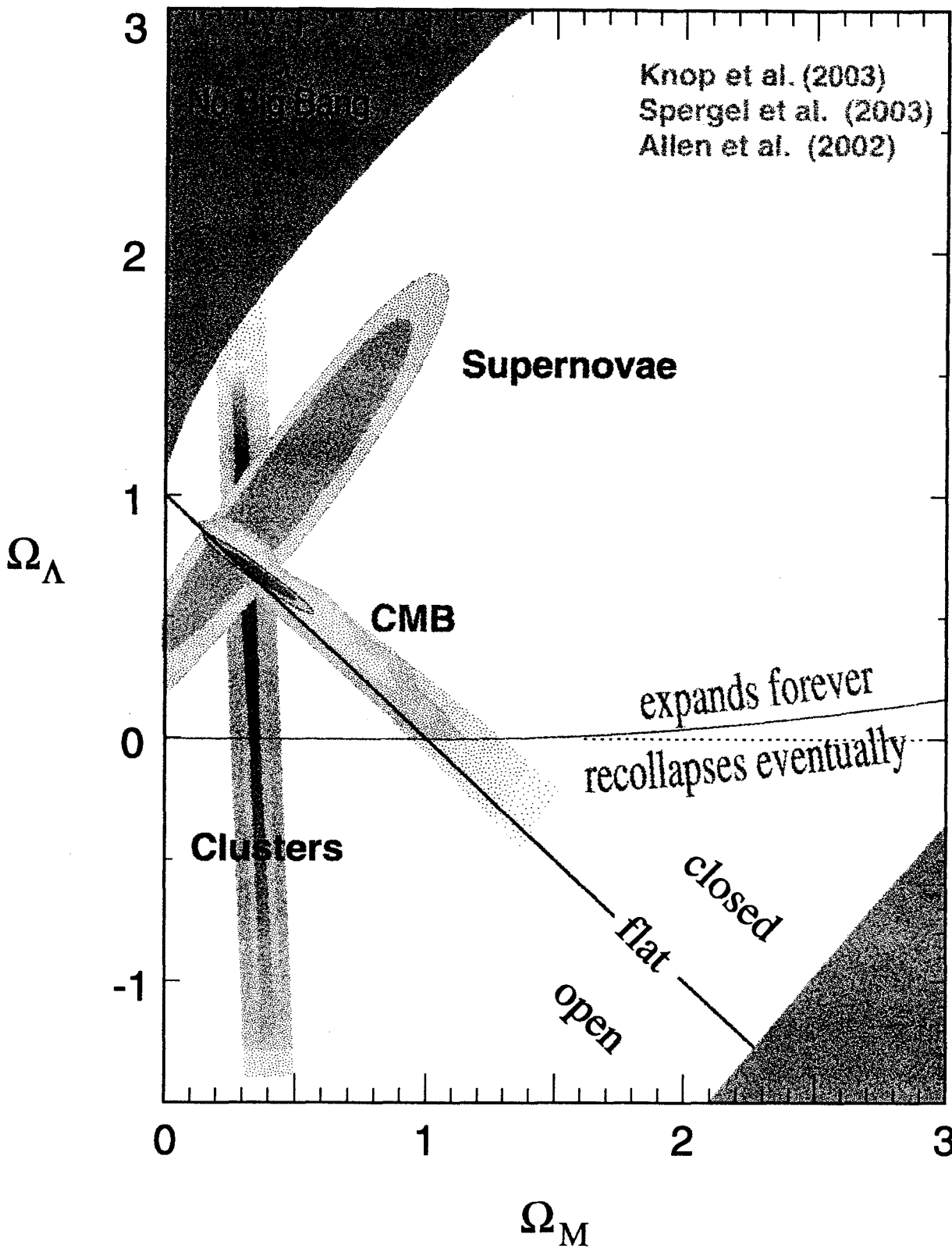
which makes equation of state

$$p = p(\rho) \text{ time-dependent!}$$

Independent check : CMB
clusters

$\Omega_\Lambda = 0.75$ best fit

Supernova Cosmology Project



$H_0 = 73 \pm 3 \frac{\text{km}}{\text{s Mpc}}$

What is the source of dark matter?
unknown light particles?

Is there a way to avoid singularity?
was the Universe evolving before?

How about unification of interactions*?
(gauge + gravity)

requires running gravitational "constant"
 $G \propto \frac{1}{\phi}$ - dilaton

Is there a quantum theory of gravity?

These questions are addressed
in more fundamental framework
than Einstein's theory

i.e.

superstring &

M-theory (brane)

* extra dimensions -
moduli fields

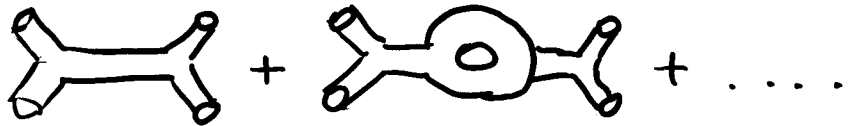
III. SUPERSTRING COSMOLOGIES

Unification requires "running" of grav. constant

$$G(t) = \frac{1}{\Phi(t)} = \frac{\lambda_s^2}{e^{-\phi(t)}} = \frac{1}{M_{pl}^2(t)} \quad \left[\frac{1}{\text{Energy}^2} \right]$$

$\lambda_s^2 \leftarrow$ fundamental string length (=const.)
 \uparrow dilaton field
 \leftarrow Planck mass
 $\Phi(t)$ Brans-Dicke field

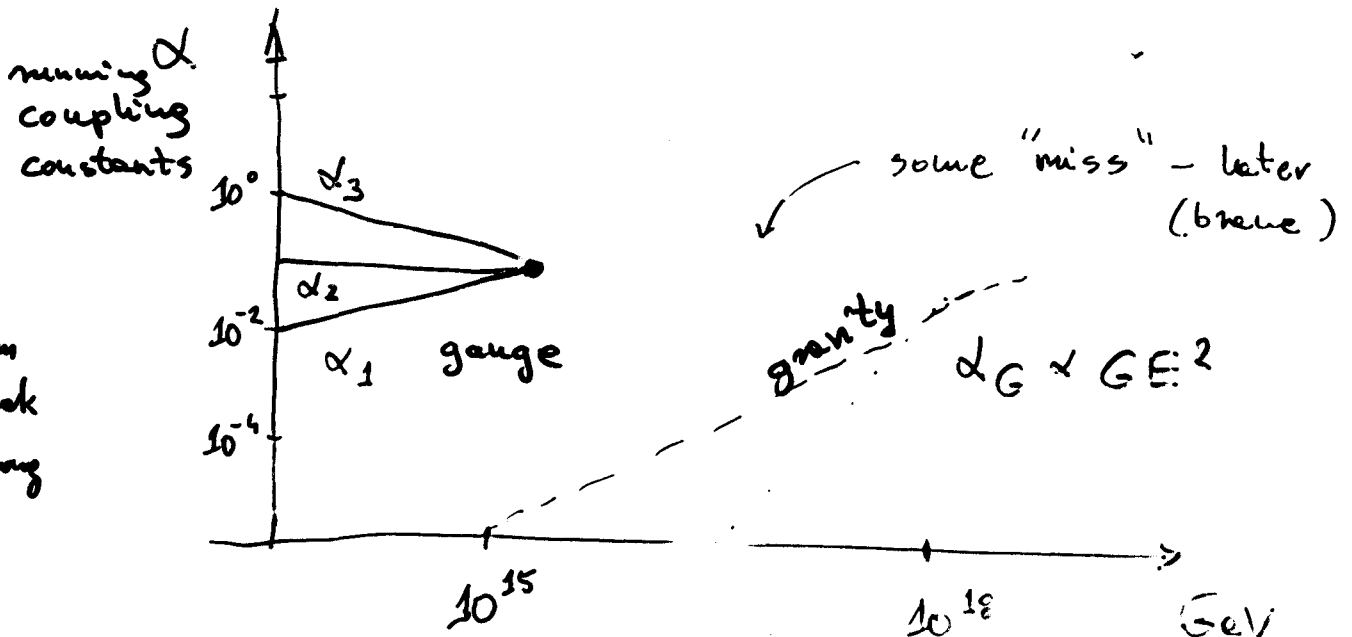
String theory interpretation



$$g_s \propto \langle e^{\phi/2} \rangle$$

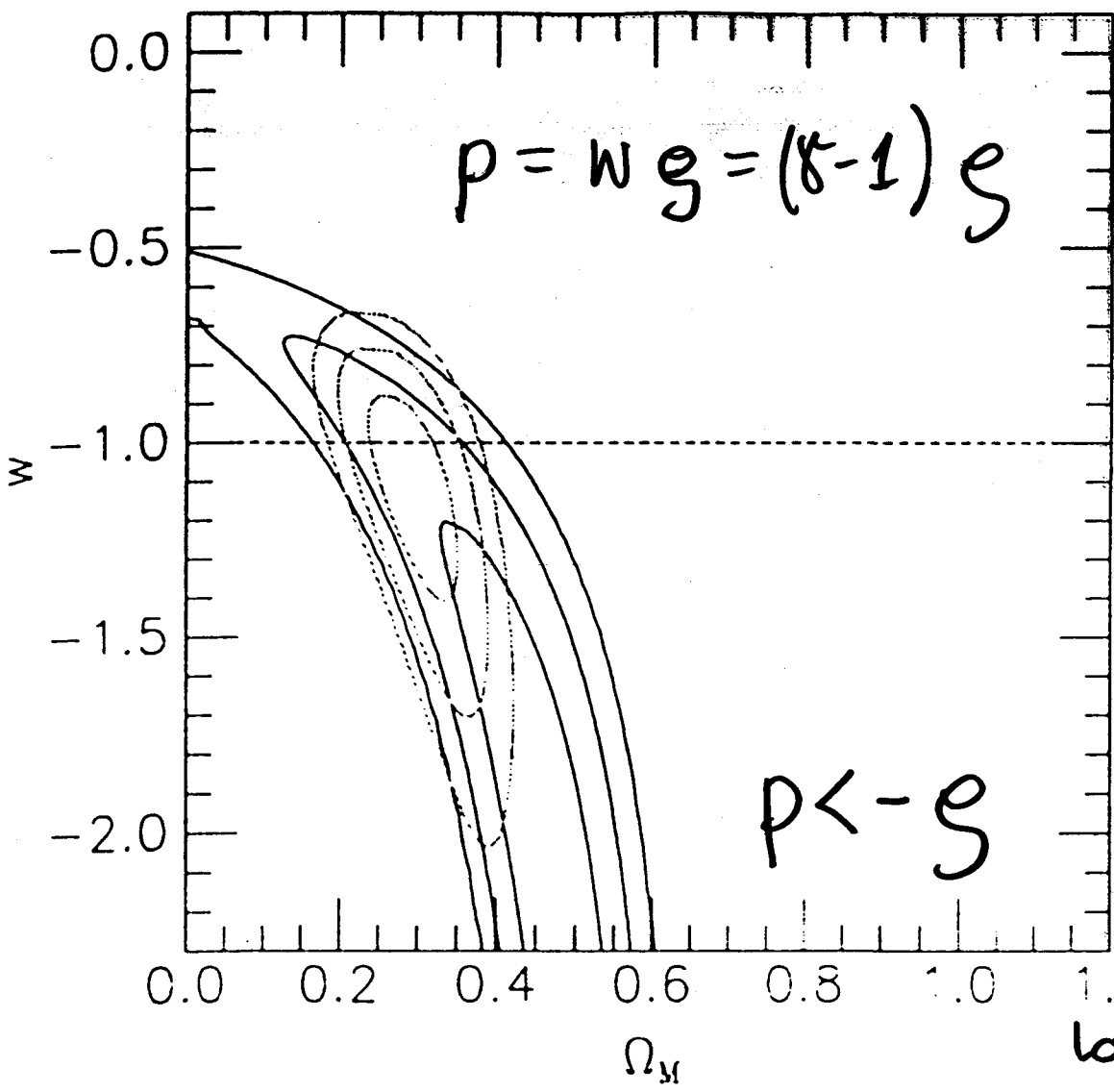
\uparrow string coupling constant

1. $\phi \rightarrow \infty$ strong coupling
2. $\phi \rightarrow -\infty$ weak coupling (perturbative)



New data

Torrey et al. astro-ph/0305008 (Ap.J. 2003)



strong evidence for very large negative pressure

Fig. 13.— Probability contours for dark energy parameter w versus Ω_m are shown at 1σ , 2σ , and 3σ when $\Omega_{tot} = 1$. We also give 1σ , 2σ , and 3σ contours when we adopt a prior of $\Omega_M h = 0.20 \pm 0.03$ from the 2dF survey (Percival et al. 2001). This sample includes all 172 SN Ia with $z > 0.01$ and $A_V < 0.5$ mag.

"phantom" (violates weak energy condition of Hawking Penrose)

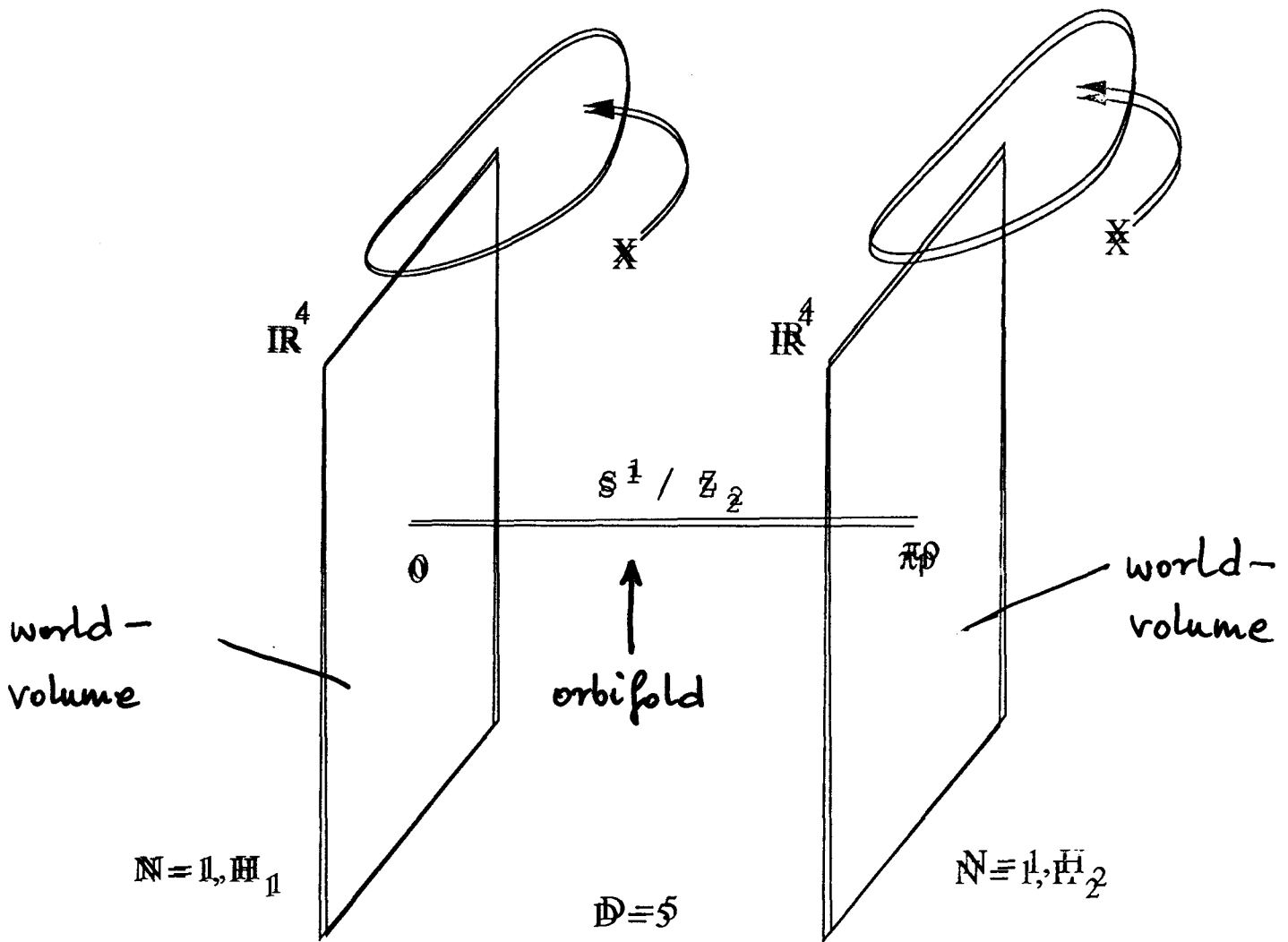


Figure 5: Horava-Witten model compactified on Calabi-Yau manifold.

similarity - (Pre-big-bang) scale factor duality
 & phantom duality

For phantom barotropic index

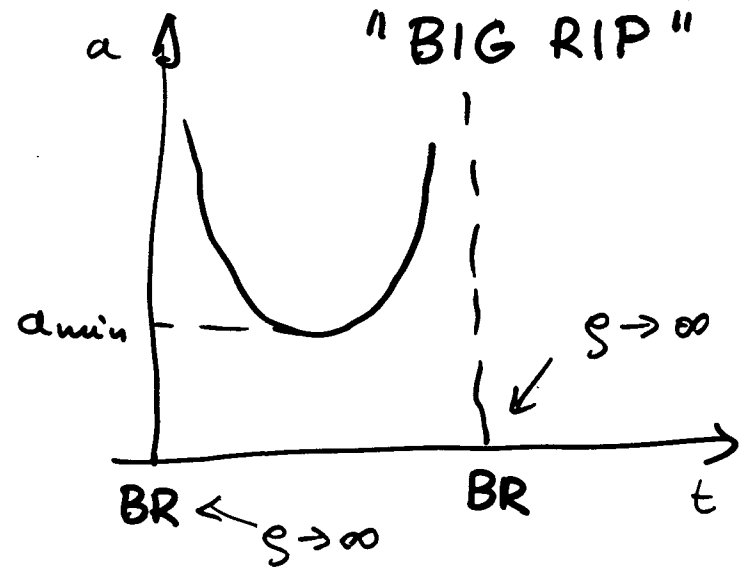
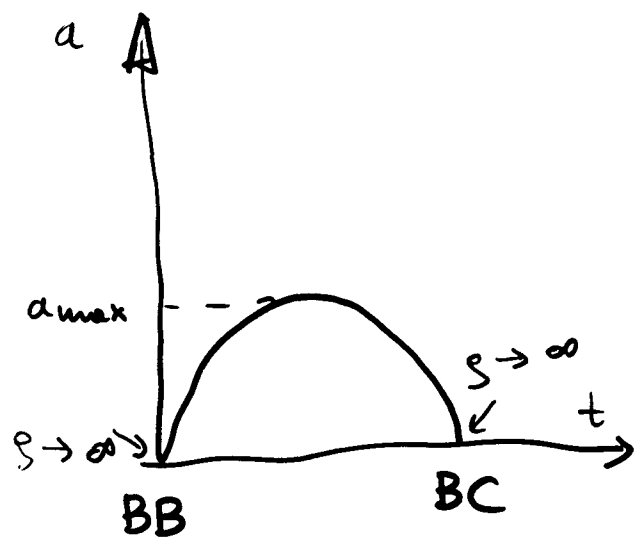
$\gamma < 0$ assume $|\gamma| = -\gamma > 0$

so that

$$\rho \propto a^{3|\gamma|}$$

the bigger the universe the denser it is - future curvature singularity

"BIG RIP"



Phantom Duality
 (field equations invariant w.r.t)

$$a \leftrightarrow \frac{1}{a}$$

$\gamma \leftrightarrow -\gamma$

Standard matter
 (including $-0.5 \leq p \leq 0$)



phantom matter
 $p < -0.5$

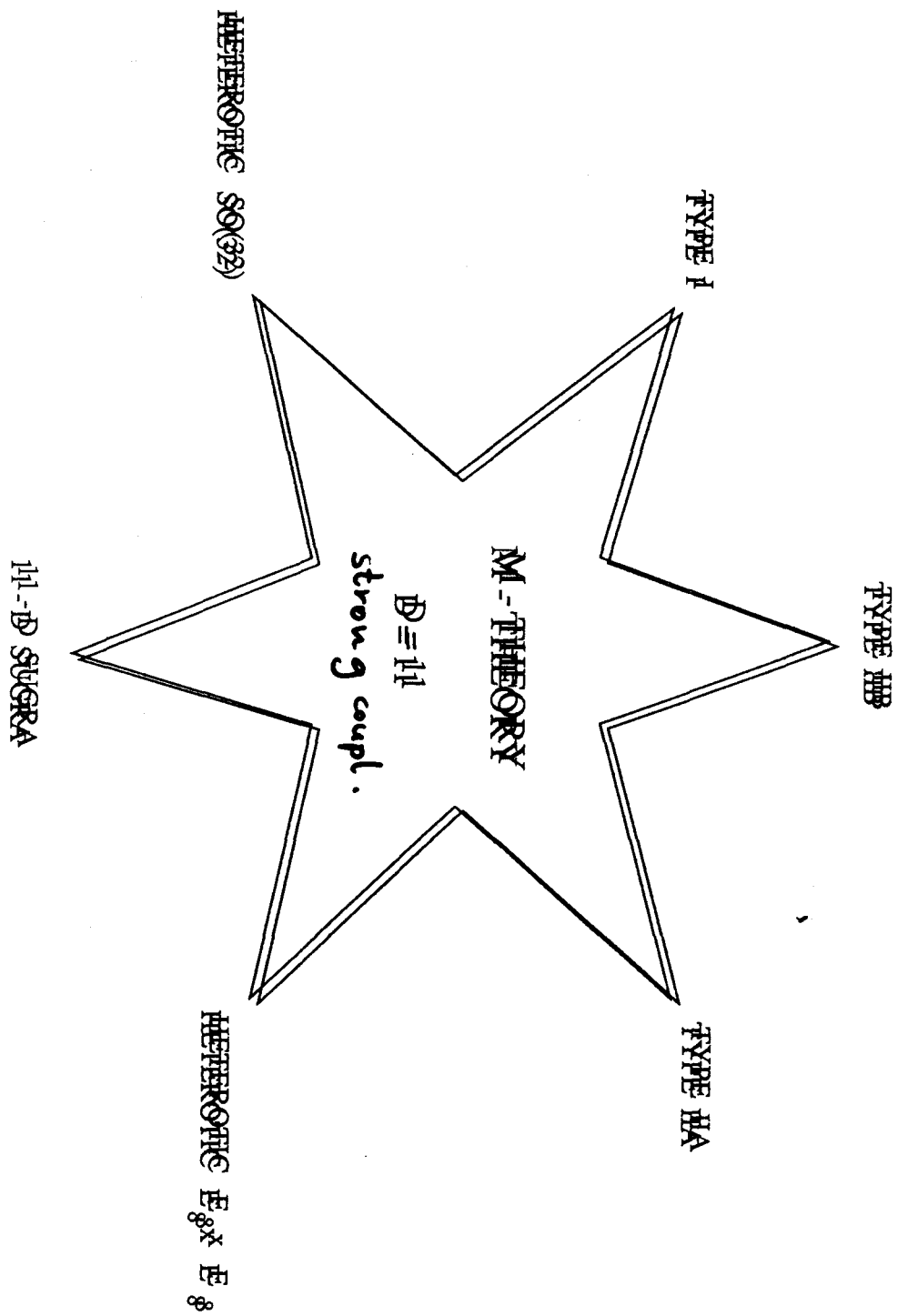


Figure 1.1: Moduli space of superstring theories.

weak coupling $\phi/2$
 $g_s = e \rightarrow 0$

strong coupling $\phi/2$
 $g_s = e \rightarrow \infty$

$g_s \leftrightarrow 1/g_s$
 duality

(7a) (6)

Prediction :

Modification of Newton's potential
in a 4-dimensional world

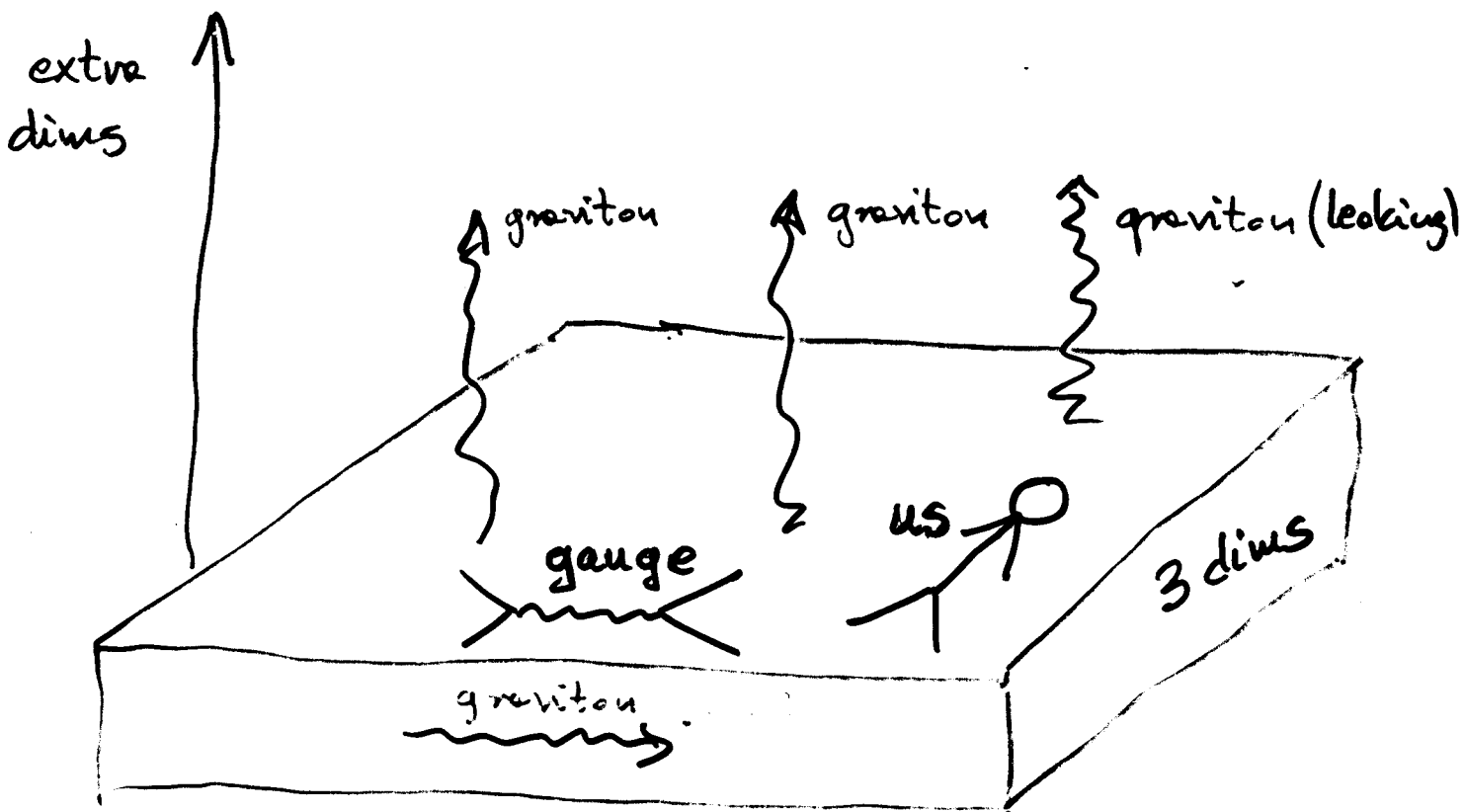
$$V(r) = \frac{GM}{r} \left(1 + \frac{2L^2}{3r^2} \right)$$

← \sim size of an extra dimension

in a submillimeter scale

$$r \leq 1 \text{ mm}$$

Explanation :



Basic cosmological solutions based on the modified Friedmann equation

$$\frac{\dot{a}^2}{a^2} = \frac{8\pi G}{3} \rho + \frac{8\pi G}{6\lambda} \rho^2 - \frac{k}{a^2} + \frac{2}{\lambda} \frac{u}{8\pi G}$$

↙
 a unique contribution from brane

↘
 dark radiation

(gravitons leaking or flowing into the brane)

$$u \lesseqgtr 0$$

(ρ^n - Condensation generalization)

λ -brane tension

Einstein limit for $\lambda \rightarrow \infty$! (in fact nucleosynth. restr.)
 $\lambda > (100\text{GeV})^4$

Types of cosmologies similar qualitatively but not quantitatively

For example: inflation requires fluid with much stronger negative pressure

$\gamma < \frac{1}{3} \frac{\rho + 2\lambda}{\rho + \lambda}$	$\lambda \rightarrow \infty$ (Einstein)	$p < -\frac{1}{3}\rho$
	λ small (brane)	$p < -\frac{2}{3}\rho$

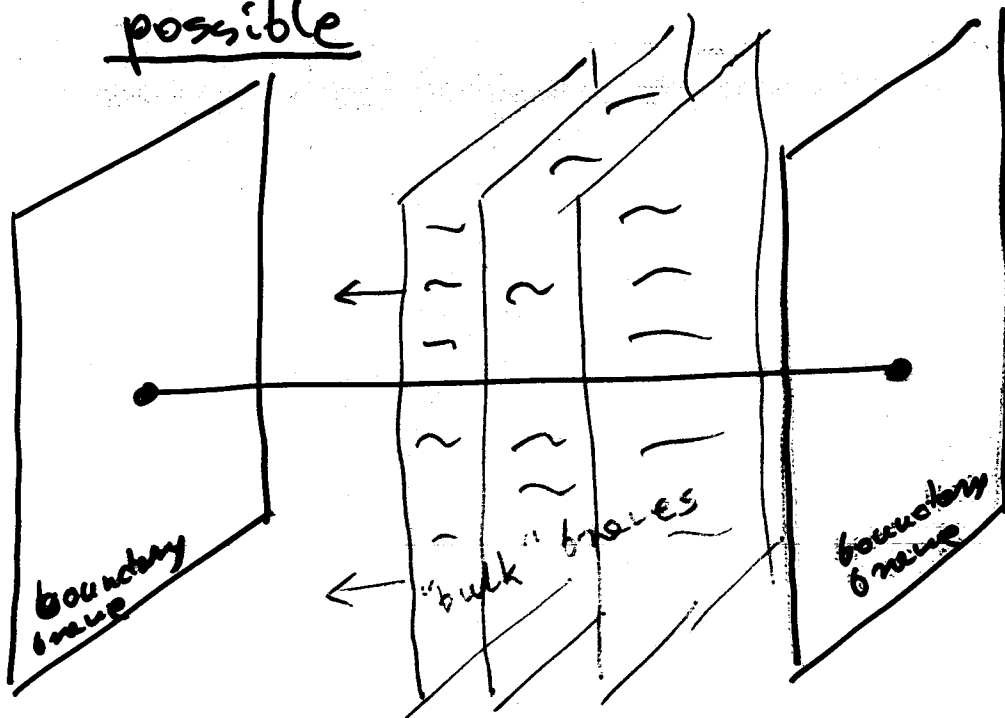
e.g. phantom required to adapt supernovae data

Ekyrotic / cyclic framework

(16)

③ Hořava-Witten theory

additional branes called "bulk" branes
which move between boundary branes
possible



a bulk brane hits a boundary brane
and "produces" Big-Bang

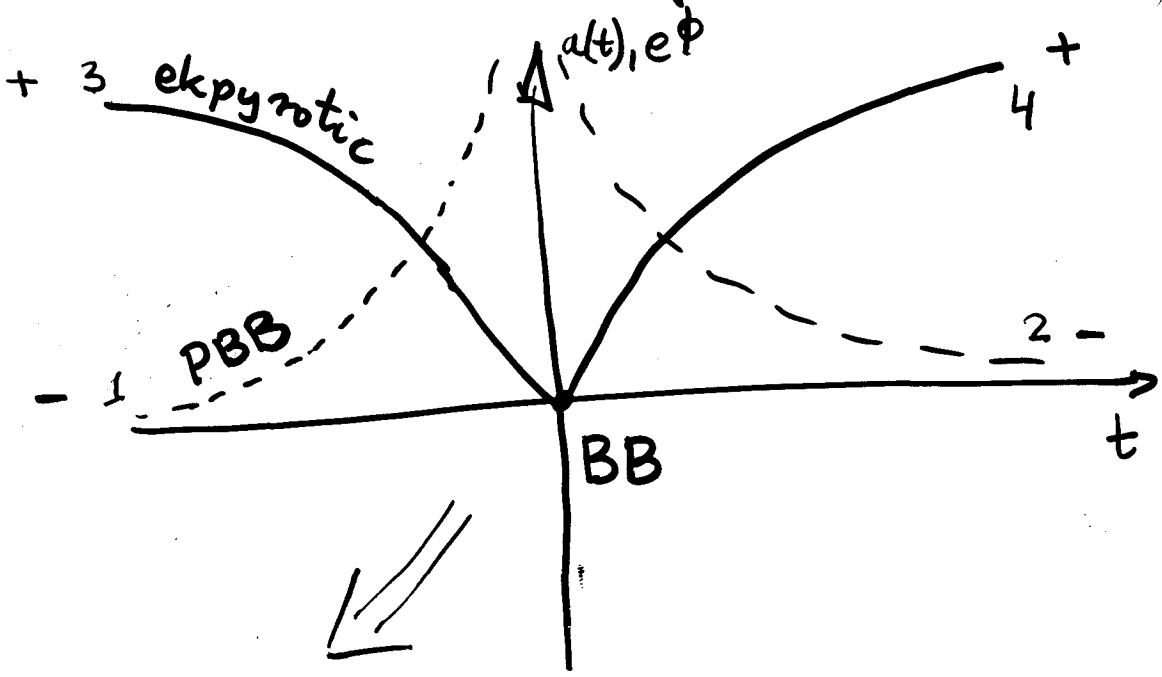
Effective 4-dim description as
in pre-big-bang, so 4 branches possible

$$a(t) = |t|^{\pm \frac{1}{3}}$$

$$\phi(t) = (\pm \sqrt{3} - 1) |t|$$

However,

one makes use of a different branch in a pre-big-bang phase



Big-Bang has no strong coupling singularity since now

$$g_s = e^\phi = |t|^{\sqrt{3}-1} \rightarrow 0$$

at t = 0

it is beneficial

but

still Big-Bang curvature singularity $\textcircled{1}$
is present

apparently - no way to go from
contraction

$$H = \frac{\dot{a}}{a} < 0$$

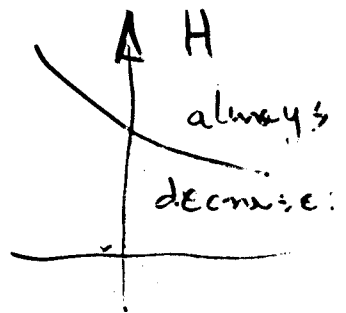
to expansion

$$H = \frac{\dot{a}}{a} > 0$$

through singularity
in 4-dim theory (H should have a minimum)

$$\dot{H} = \left(\frac{\dot{a}}{a}\right)^{\cdot} = -4\pi G(\rho + p)$$

$$= -4\pi G \dot{\phi}^2 \leq 0$$



unless one violates

the weak energy condition $\rho + p \geq 0$

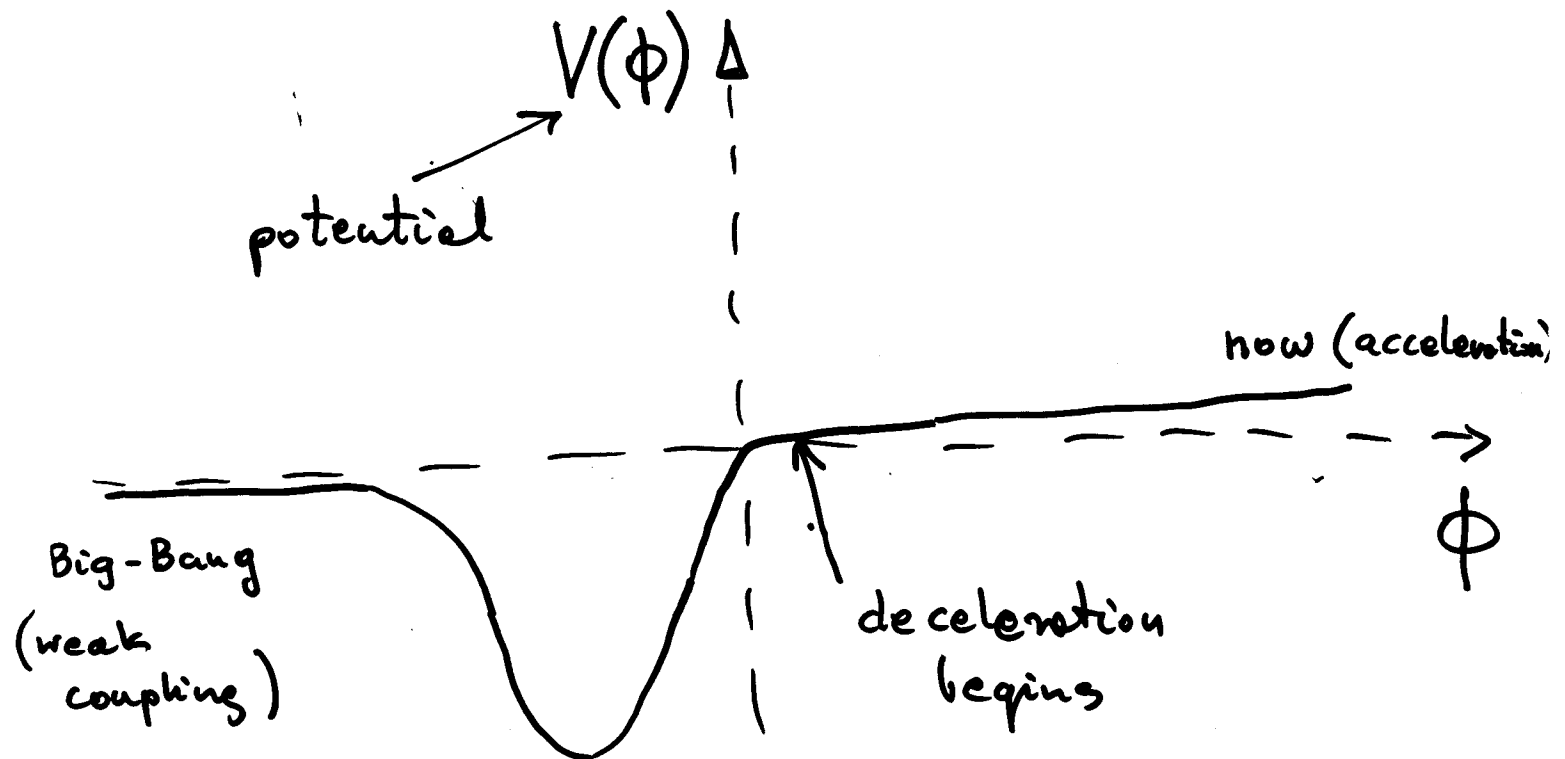
in fact, phantom does

and, in principle, possible

Denying phantom, still the singularity ⁽¹⁹⁾
avoidance possible due to a special
 choice of the potential and coupling
 to an energy-momentum tensor

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{16\pi G} R - \frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) + \beta^4(\phi) (S_R + S_m) \right]$$

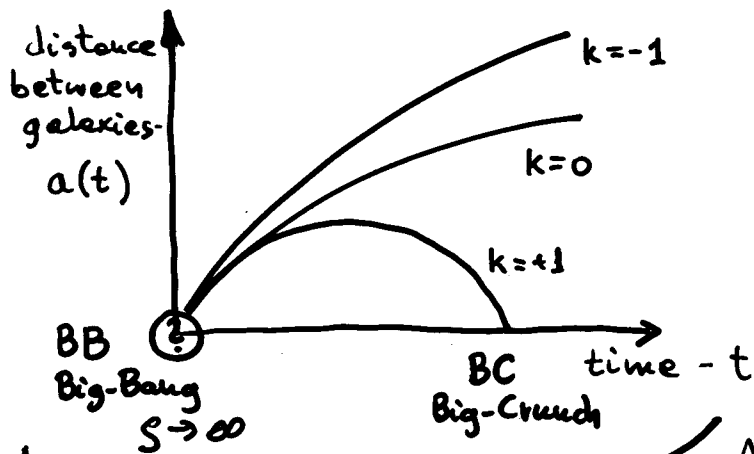
coupling ← ↓ radiation ↘ matter



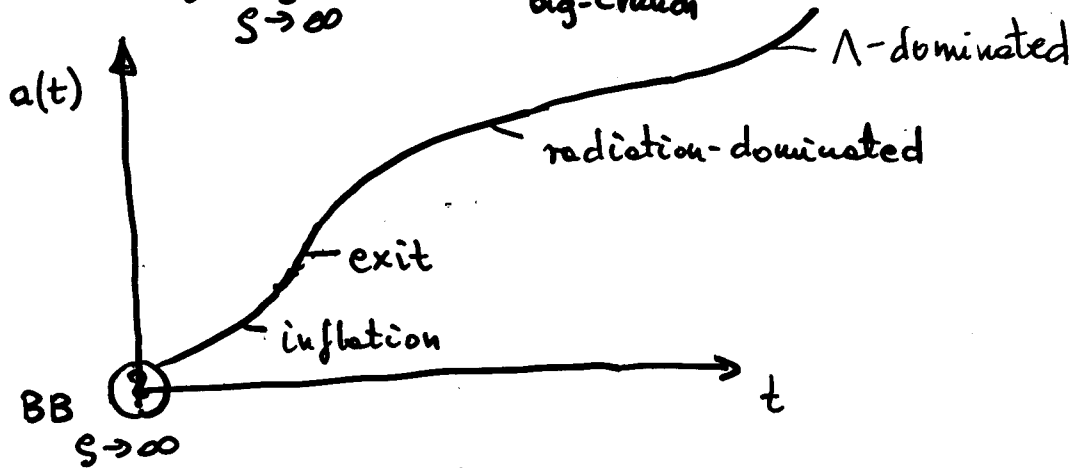
$$V(\phi) = V_0 (1 - e^{-c\phi}) F(\phi), \quad F(\phi) \propto e^{-\frac{1}{g_s} \phi}$$

BASIC COSMOLOGIES

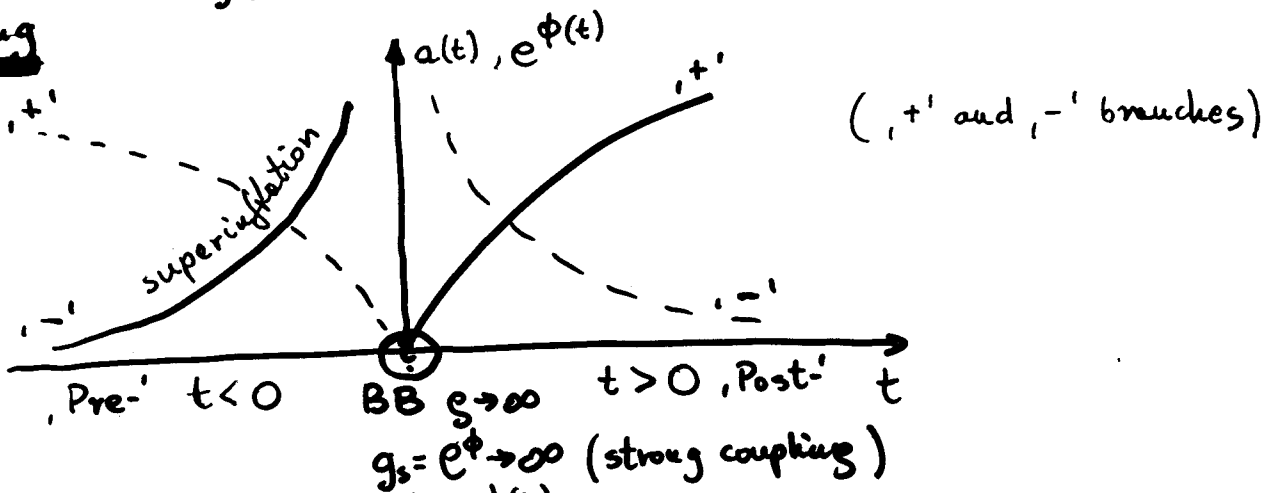
Standard



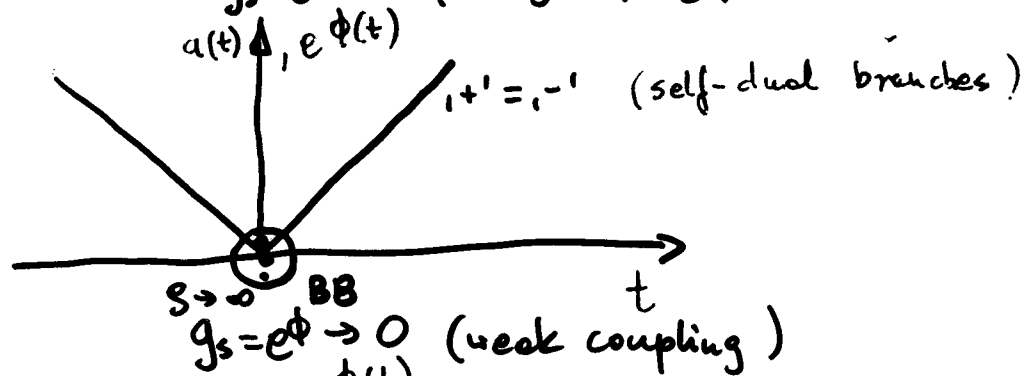
Inflationary



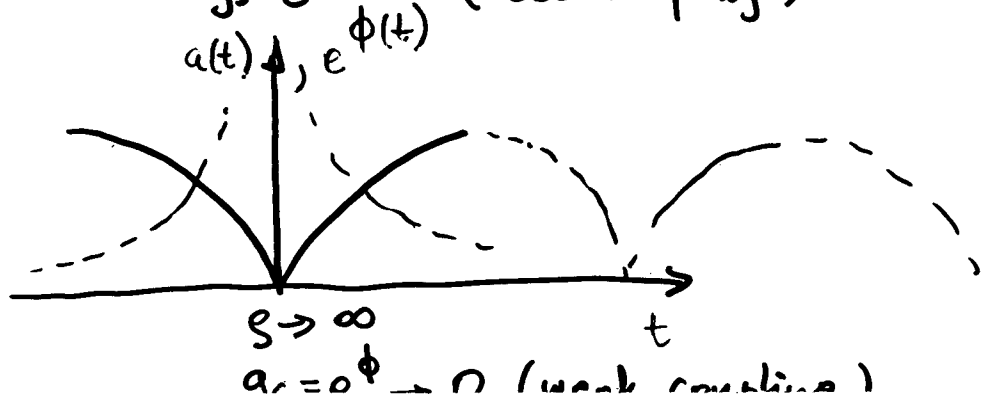
Pre-Big-Bang (superstring) $\omega = -1$



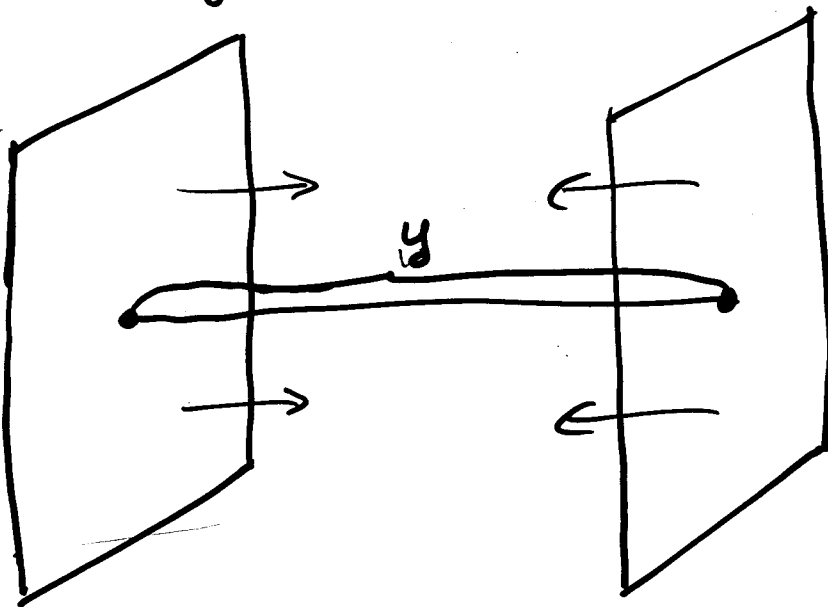
Conformal Relativity $\omega = -\frac{2}{3}$



Cyclic (M-theory)



Scenario admissible only for
collision of boundary branes (not bulk branes)



The 5th dimension y (orbifold) collapses
 but 4-dim theory has no singularity

generalized
 Friedman

$$H^2 = \frac{8\pi G}{3} \left(\frac{1}{2} \dot{\phi}^2 + V + \beta^4 \rho_R + \beta^4 \rho_M \right)$$

$$\frac{\ddot{a}}{a} = -\frac{8\pi G}{3} \left(\dot{\phi}^2 + V + \beta^4 \rho_R + \frac{1}{2} \beta^2 \rho_M \right)$$

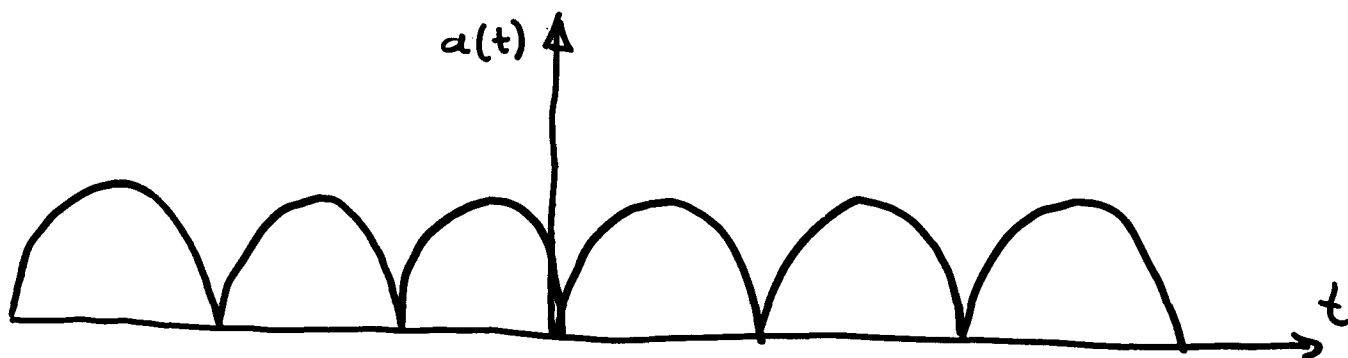
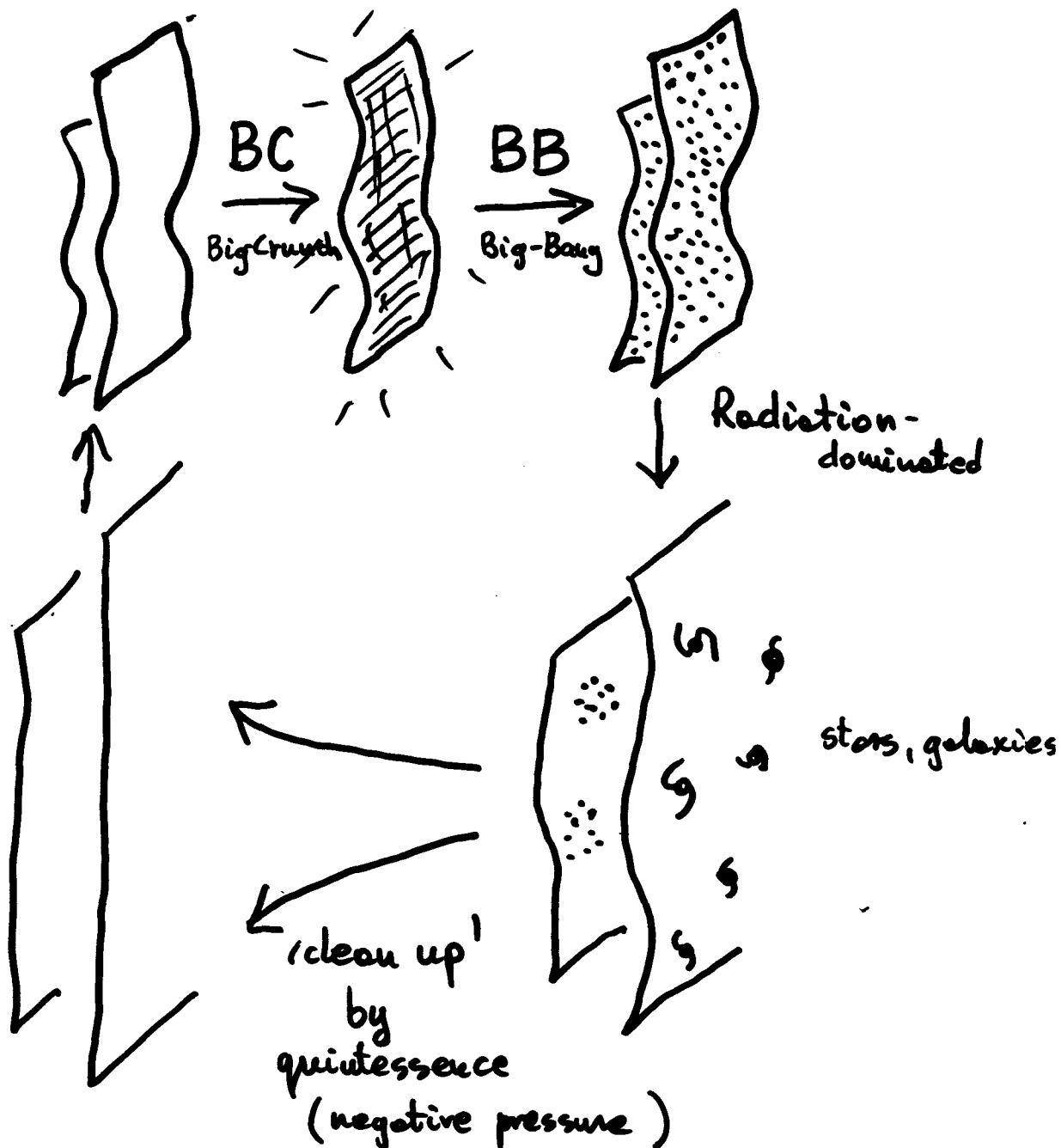
since

$$\rho_R \sim \frac{1}{[a\beta(\phi)]^4} \stackrel{a \rightarrow 0}{\sim} \frac{1}{\left(a \frac{1}{a}\right)^3} \sim \text{const.}$$

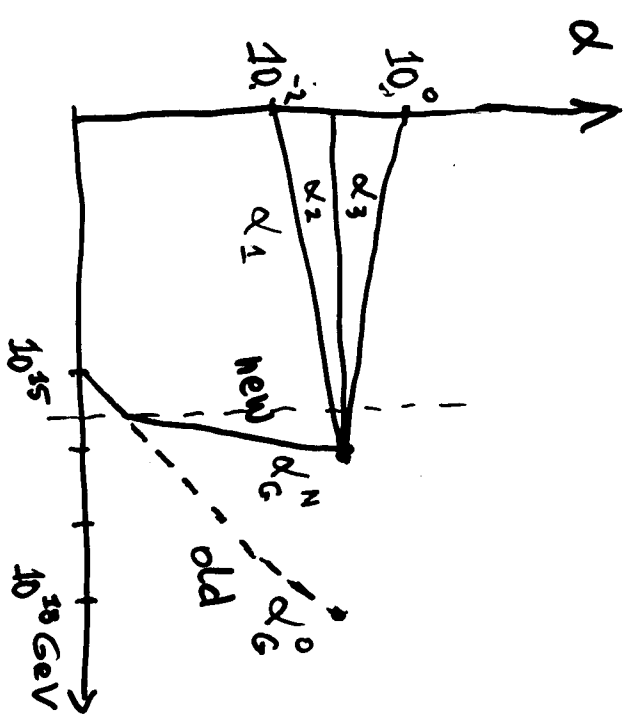
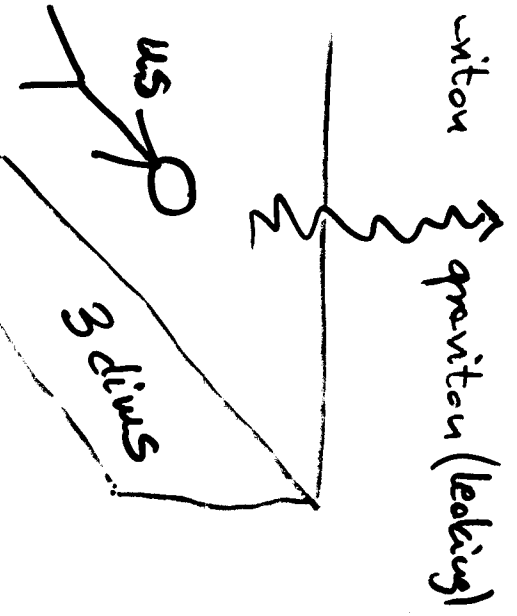
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CYCLIC (RECYCLING) UNIVERSE

Based on M-theory - colliding 3-branes in 5-dimensional spacetime.



world \leftarrow size of an extra dimension
 $\frac{2L^2}{3V^2}$
 scale



Randall-Sundrum (1999)
 framework
 Arkani-Hamed, Dimde 198
 & others

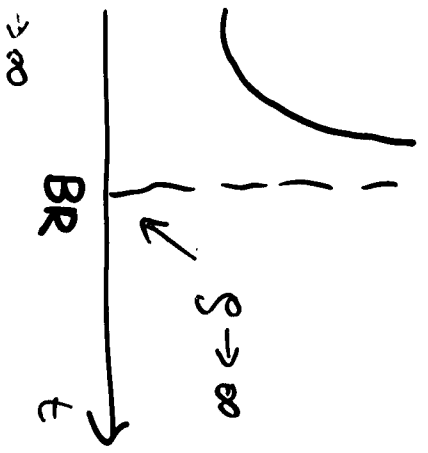
meet
provided
 one admits gravity propagates in a different number of dimensions than gauge interactions
 (unification at 10^{16} GeV)

the scale of unification of gravity can even be lowered to electroweak
 10^{16} eV
 energy scale

GRAVITY IS WEAK NOW COMPARED TO OTHER INTERACTIONS SINCE SOME

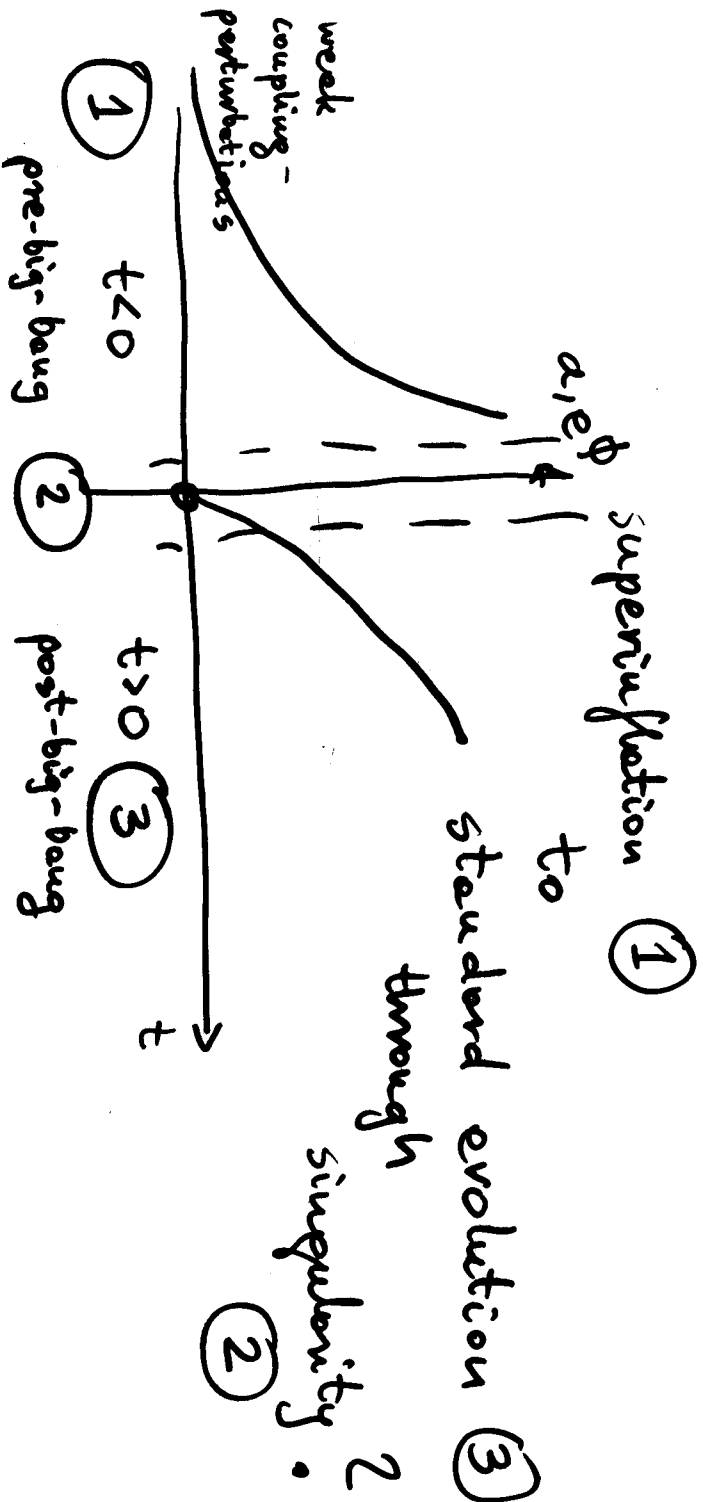
$$|R| = -R > 0$$

the bigger the universe the denser it is - future universe singularity "BIG RIP"



"Graceful-exit" problem

How to transit from



Possible solutions:

1. Regularize singularity in sense of string theory
 - Λ_s effects
 - loops effects

2. Quantum mechanical tunneling through singularity

phantom

V. CONCLUSIONS

Hot points:

- Universe accelerates -
all "exotics" admissible
to explain this
 - quintessence
 - phantom
 - cordassian
 - Chaplygin gas etc
- theories which move
"before" Big-Bang under studies
- non-singular/cyclic universes
possible

(cf. no black hole
claim of
yesterday)