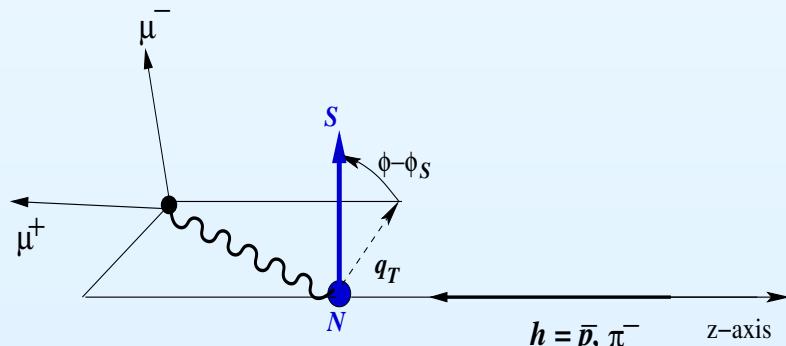
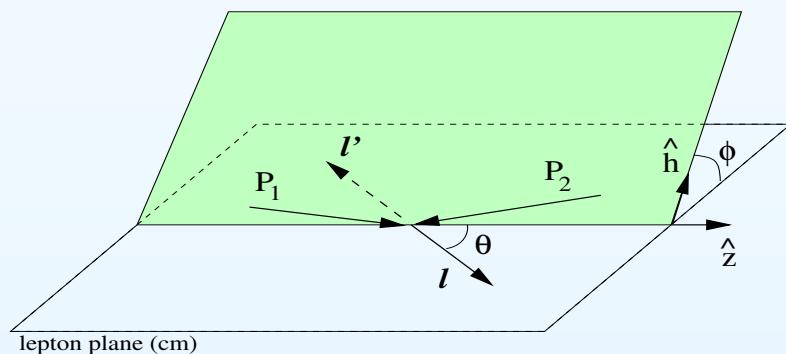
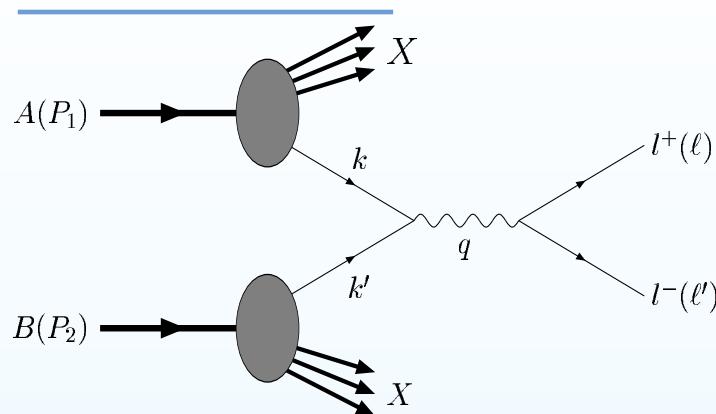


TRANSVERSITY AND ITS ACCOMPANYING T-ODD DISTRIBUTION FROM UNPOLARIZED AND SINGLE-POLARIZED DRELL-YAN PROCESSES

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Kinematics



- $x_1 = \frac{Q^2}{2p_1 q}, \quad x_2 = \frac{Q^2}{2p_2 q}$ – fractions of the longitudinal momentum of the hadrons A and B carried by the quark and antiquark which annihilate into virtual photon
- $s = (p_1 + p_2)^2 \simeq 2p_1 p_2$ – the center of mass energy squared

$$Q^2 = M^2 \simeq x_1 x_2 s \equiv \tau s$$

$$y = \frac{1}{2} \ln \frac{x_1}{x_2}$$

$$x_f = x_1 - x_2$$

$$x_1 = \frac{\sqrt{x_f^2 + 4\tau} + x_F}{2} = \sqrt{\tau} \exp^y$$

$$x_2 = \frac{\sqrt{x_f^2 + 4\tau} - x_F}{2} = \sqrt{\tau} \exp^{-y}$$
- θ – production angle in the dilepton rest frame – polar angle of the lepton pair in the dilepton rest frame
- ϕ – azimuthal angle of lepton pair
- ϕ_S – azimuthal angle of the hadron polarization measured with respect to lepton plane

Cross-sections

QPM: (D. Boer, PRD 60 (1999) 014012)

Unpolarized DY: $H_1 H_2 \rightarrow l^+ l^- X$

$$\frac{d\sigma^{(0)}(H_1 H_2 \rightarrow l \bar{l} X)}{d\Omega dx_1 dx_2 d^2 \mathbf{q}_T} = \frac{\alpha^2}{12 Q^2} \sum_q e_q^2 \left\{ (1 + \cos^2 \theta) \mathcal{F}[\bar{f}_{1q} f_{1q}] + \sin^2 \theta \cos(2\phi) \mathcal{F} \left[(2 \hat{\mathbf{h}} \cdot \mathbf{k}_{1T} \hat{\mathbf{h}} \cdot \mathbf{k}_{2T} - \mathbf{k}_{1T} \cdot \mathbf{k}_{2T}) \frac{\bar{h}_{1q}^\perp h_{1q}^\perp}{M_1 M_2} \right] \right\}$$

Single polarized DY: $H_1 H_2^\uparrow \rightarrow l^+ l^- X$

PAX: $\bar{p} p^\uparrow \rightarrow e^+ e^- X$

COMPASS: $\pi^- p^\uparrow \rightarrow \mu^+ \mu^- X$

$$\begin{aligned} \frac{d\sigma^{(1)}(H_1 H_2^\uparrow \rightarrow l \bar{l} X)}{d\Omega dx_1 dx_2 d^2 \mathbf{q}_T} &= \frac{\alpha^2}{12 Q^2} \sum_q e_q^2 \left\{ (1 + \cos^2 \theta) \mathcal{F}[f_1 \bar{f}_1] \right. \\ &\quad \left. + \sin^2 \theta \cos(2\phi) \mathcal{F} \left[(2 \hat{\mathbf{h}} \cdot \mathbf{k}_{1T} \hat{\mathbf{h}} \cdot \mathbf{k}_{2T} - \mathbf{k}_{1T} \cdot \mathbf{k}_{2T}) \frac{h_{1q}^\perp \bar{h}_{1q}^\perp}{M_1 M_2} \right] \right. \\ &\quad \left. + (1 + \cos^2 \theta) \sin(\phi - \phi_{S_1}) \mathcal{F} \left[\hat{\mathbf{h}} \cdot \mathbf{k}_{1T} \frac{f_{1T}^\perp \bar{f}_1}{M_1} \right] - \sin^2 \theta \sin(\phi + \phi_{S_1}) \mathcal{F} \left[\hat{\mathbf{h}} \cdot \mathbf{k}_{2T} \frac{h_{1q}^\perp \bar{h}_{1q}^\perp}{M_2} \right] \right\} \end{aligned}$$

$$\hat{\mathbf{h}} \equiv \mathbf{q}_T / |\mathbf{q}_T|$$

$$\mathcal{F}[f \bar{f}] \equiv \int d^2 \mathbf{k}_{1T} d^2 \mathbf{k}_{2T} \delta^2(\mathbf{k}_{1T} + \mathbf{k}_{2T} - \mathbf{q}_T) f_q(x_1, \mathbf{k}_{1T}^2) \bar{f}_q(x_2, \mathbf{k}_{2T}^2)$$

Unpolarized DY $H_1 H_2 \rightarrow l^+ l^- X$

$$\frac{d\sigma^{(0)}(H_1 H_2 \rightarrow l \bar{l} X)}{d\Omega dx_1 dx_2 d^2 \mathbf{q}_T} = \frac{\alpha^2}{12Q^2} \sum_q e_q^2 \left\{ (1 + \cos^2 \theta) \mathcal{F}[\bar{f}_{1q} f_{1q}] + \sin^2 \theta \cos(2\phi) \mathcal{F} \left[(2 \hat{\mathbf{h}} \cdot \mathbf{k}_{1T} \hat{\mathbf{h}} \cdot \mathbf{k}_{2T} - \mathbf{k}_{1T} \cdot \mathbf{k}_{2T}) \frac{\bar{h}_{1q}^\perp h_{1q}^\perp}{M_1 M_2} \right] \right\}$$

$$\begin{aligned} R &= \frac{3}{16\pi} (1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi \\ &+ k \sin^2 \theta \cos 2\phi), \quad (\lambda \simeq 1, \mu \simeq 0, k \equiv \nu/2) \end{aligned}$$

$$h_{1q}^\perp(x, \mathbf{p}_T^2) = \frac{\alpha_T}{\pi} \frac{M_C M_H}{\mathbf{p}_T^2 + M_C^2} e^{-\alpha_T \mathbf{p}_T^2} f_{1q}(x) \quad (\mathbb{M}_c = 2.3 \text{ GeV}, \alpha_T = 1 \text{ GeV}^{-2})$$

q_T integration approach

- e^+e^- annihilation: D. Boer, R. Jakob, P.J. Mulders, NPB **504**, 345 (1997); PLB **424**, 143 (1998)
- SIDIS: D. Boer, P.J. Mulders, PRD **57**, 5780 (1998)

We introduce [hep-ph/0505214, Phys. Rev. D (to be published)]

$$\hat{R} = \frac{\int d^2\mathbf{q}_T [|\mathbf{q}_T|^2/M_1 M_2] [d\sigma^{(0)}/d\Omega]}{\int d^2\mathbf{q}_T \sigma^{(0)}},$$
$$\hat{R} = \frac{3}{16\pi} (\gamma(1+\cos^2\theta) + \hat{k} \sin^2\theta \cos 2\phi)$$

Factorization

$$\hat{k} = \frac{\int d^2\mathbf{q}_T [\mathbf{q}_T^2/M_1 M_2] \sum_q e_q^2 \mathcal{F}[(2\hat{\mathbf{h}} \cdot \mathbf{k}_{1T} \hat{\mathbf{h}} \cdot \mathbf{k}_{2T} - \mathbf{k}_{1T} \cdot \mathbf{k}_{2T}) \frac{\bar{h}_1^\perp h_1^\perp}{M_1 M_2}]}{\int d^2\mathbf{q}_T \sum_q e_q^2 \mathcal{F}[\bar{f}_1 f_1]}$$

$$\mathcal{F}[f \bar{f}] \equiv \int d^2\mathbf{k}_{1T} d^2\mathbf{k}_{2T} \delta^2(\mathbf{k}_{1T} + \mathbf{k}_{2T} - \mathbf{q}_T) f_q(x_1, \mathbf{k}_{1T}^2) \bar{f}_q(x_2, \mathbf{k}_{2T}^2)$$

$$\begin{aligned} & \delta^2(\mathbf{k}_{1T} + \mathbf{k}_{2T} - \mathbf{q}_T) (2 \frac{(\mathbf{q}_T \mathbf{k}_{1T})(\mathbf{q}_T \mathbf{k}_{2T})}{\mathbf{q}_T^2} - \mathbf{k}_{1T} \mathbf{k}_{2T}) \mathbf{q}_T^2 \\ &= 2 \mathbf{k}_{1T}^2 \mathbf{k}_{2T}^2 + \frac{\mathbf{k}_{1T}^2 (\mathbf{k}_{1T} \mathbf{k}_{2T})}{\downarrow} + \frac{\mathbf{k}_{2T}^2 (\mathbf{k}_{1T} \mathbf{k}_{2T})}{\downarrow} + 2(\mathbf{k}_{1T} \mathbf{k}_{2T})^2 - 2(\mathbf{k}_{1T} \mathbf{k}_{2T})^2 \end{aligned}$$

$$\hat{k} = 8 \frac{\sum_q e_q^2 (\bar{h}_{1q}^{\perp(1)}(x_1) h_{1q}^{\perp(1)}(x_2) + (1 \leftrightarrow 2))}{\sum_q e_q^2 (\bar{f}_{1q}(x_1) f_{1q}(x_2) + (1 \leftrightarrow 2))}$$

$$h_{1q}^{\perp(n)}(x) \equiv \int d^2\mathbf{k}_T \left(\frac{\mathbf{k}_T^2}{2M^2} \right)^n h_{1q}^\perp(x, \mathbf{k}_T^2)$$

Single polarized DY process $H_1 H_2^\uparrow \rightarrow l^+ l^- X$

$$\begin{aligned}
\frac{d\sigma^{(1)}(H_1 H_2^\uparrow \rightarrow l \bar{l} X)}{d\Omega dx_1 dx_2 d^2 \mathbf{q}_T} = & \frac{\alpha^2}{12Q^2} \sum_q e_q^2 \left\{ (1 + \cos^2 \theta) \mathcal{F}[f_1 \bar{f}_1] \right. \\
& + \sin^2 \theta \cos(2\phi) \mathcal{F} \left[(2 \hat{\mathbf{h}} \cdot \mathbf{k}_{1T} \hat{\mathbf{h}} \cdot \mathbf{k}_{2T} - \mathbf{k}_{1T} \cdot \mathbf{k}_{2T}) \frac{h_1^\perp \bar{h}_1^\perp}{M_1 M_2} \right] \\
& + (1 + \cos^2 \theta) \sin(\phi - \phi_{S_1}) \mathcal{F} \left[\hat{\mathbf{h}} \cdot \mathbf{k}_{1T} \frac{f_{1T}^\perp \bar{f}_1}{M_1} \right] \\
& \left. - \sin^2 \theta \sin(\phi + \phi_{S_1}) \mathcal{F} \left[\hat{\mathbf{h}} \cdot \mathbf{k}_{2T} \frac{h_1 \bar{h}_1^\perp}{M_2} \right] \right\}
\end{aligned}$$

Let us consider SSA

$$\begin{aligned}
\hat{A}_{\mathbf{h}(f)} &= \frac{\int d\Omega d\phi_{S_2} \sin(\phi \pm \phi_{S_2}) [d\sigma(\mathbf{S}_{2T}) - d\sigma(-\mathbf{S}_{2T})]}{\int d\Omega d\phi_{S_2} [d\sigma(\mathbf{S}_{2T}) + d\sigma(-\mathbf{S}_{2T})]} \\
A_{\mathbf{h}} &= -\frac{1}{4} \frac{\sum_q e_q^2 \mathcal{F} \left[\frac{\hat{\mathbf{h}} \cdot \mathbf{k}_{1T}}{M_1} \bar{h}_{1q}^\perp h_{1q} \right]}{\sum_q e_q^2 \mathcal{F} [\bar{f}_{1q} f_{1q}]} , \quad A_f = \frac{1}{2} \frac{\sum_q e_q^2 \mathcal{F} \left[\frac{\hat{\mathbf{h}} \cdot \mathbf{k}_{2T}}{M_2} \bar{f}_1^q f_{1T}^{\perp q} \right]}{\sum_q e_q^2 \mathcal{F} [\bar{f}_{1q} f_{1q}]}
\end{aligned}$$



Should be studied



Anselmino et al (PRD, 2003), Efremov et al (PRD, 2004)

Factorization

By analogy with $A_{UT}^{\sin(\phi-\phi_S)\frac{qT}{M_N}}$ considered in ref. A.V.

Efremov et al, PLB **612** (2005) 233, we introduce

$$\hat{A}_h = \frac{\int d\Omega d\phi_{S_2} \int d^2\mathbf{q}_T (|\mathbf{q}_T|/M_1) \sin(\phi+\phi_{S_2}) [d\sigma(\mathbf{S}_{2T}) - d\sigma(-\mathbf{S}_{2T})]}{\int d\Omega d\phi_{S_2} \int d^2\mathbf{q}_T [d\sigma(\mathbf{S}_{2T}) + d\sigma(-\mathbf{S}_{2T})]}$$

so that after integration

$$\hat{A}_h = -\frac{1}{2} \frac{\sum_q e_q^2 [\bar{h}_{1q}^{\perp(1)}(x_1) h_{1q}(x_2) + (1 \leftrightarrow 2)]}{\sum_q e_q^2 [\bar{f}_{1q}(x_1) f_{1q}(x_2) + (1 \leftrightarrow 2)]},$$

$$h_{1q}^{\perp(1)}(x) \equiv \int d^2\mathbf{k}_T \left(\frac{\mathbf{k}_T^2}{2M^2} \right) h_{1q}^\perp(x, \mathbf{k}_T^2)$$

$\bar{p}p \rightarrow l^+l^-X$ and $\bar{p}p^\uparrow \rightarrow l^+l^-X$

By virtue of charge conjugation symmetry:

$$\hat{k}|_{\bar{p}p \rightarrow l^+l^-X} = 8 \frac{\sum_q e_q^2 [h_{1q}^{\perp(1)}(x_1)h_{1q}^{\perp(1)}(x_2) + \bar{h}_{1q}^{\perp(1)}(x_1)\bar{h}_{1q}^{\perp(1)}(x_2)]}{\sum_q e_q^2 [f_{1q}(x_1)f_{1q}(x_2) + \bar{f}_{1q}(x_1)\bar{f}_{1q}(x_2)]},$$

$$\hat{A}_h|_{\bar{p}p^\uparrow \rightarrow l^+l^-X} = -\frac{1}{2} \frac{\sum_q e_q^2 [h_{1q}^{\perp(1)}(x_1)h_{1q}(x_2) + \bar{h}_{1q}(x_1)\bar{h}_{1q}^{\perp(1)}(x_2)]}{\sum_q e_q^2 [f_{1q}(x_1)f_{1q}(x_2) + \bar{f}_{1q}(x_1)\bar{f}_{1q}(x_2)]},$$

where now all PDF *refer to protons*. Neglecting squared antiquark and strange quark PDF contributions to proton and taking into account the quark charges and u quark dominance at large x , we get

$$\hat{k}(x_1, x_2)|_{\bar{p}p \rightarrow l^+l^-X} \simeq 8 \frac{h_{1u}^{\perp(1)}(x_1)h_{1u}^{\perp(1)}(x_2)}{f_{1u}(x_1)f_{1u}(x_2)},$$

$$\hat{A}_h(x_1, x_2)|_{\bar{p}p^\uparrow \rightarrow l^+l^-X} \simeq -\frac{1}{2} \frac{h_{1u}^{\perp(1)}(x_1)h_{1u}(x_2)}{f_{1u}(x_1)f_{1u}(x_2)}.$$

Upper bounds on \hat{k} , $h_{1u}^{\perp(1)}$ and \hat{A}_h

$$x_1 \simeq x_2 \simeq \sqrt{Q^2/s} \quad (x_F \simeq 0)$$

- $(|\mathbf{k}_T|/M)h_1^\perp(x, \mathbf{k}_T^2) \leq f_1(x, \mathbf{k}_T^2)$ (A. Bacchetta et al. PRL **85**, 712 (2000))

$$\langle k_T \rangle \simeq 0.8 \text{ GeV} \quad (\text{A.V. Efremov et al, PLB } \mathbf{612}, 233 \text{ (2005)})$$

$$h_{1u}^{\perp(1)} \lesssim 0.4 f_{1u}(x).$$

- Soffer inequality:

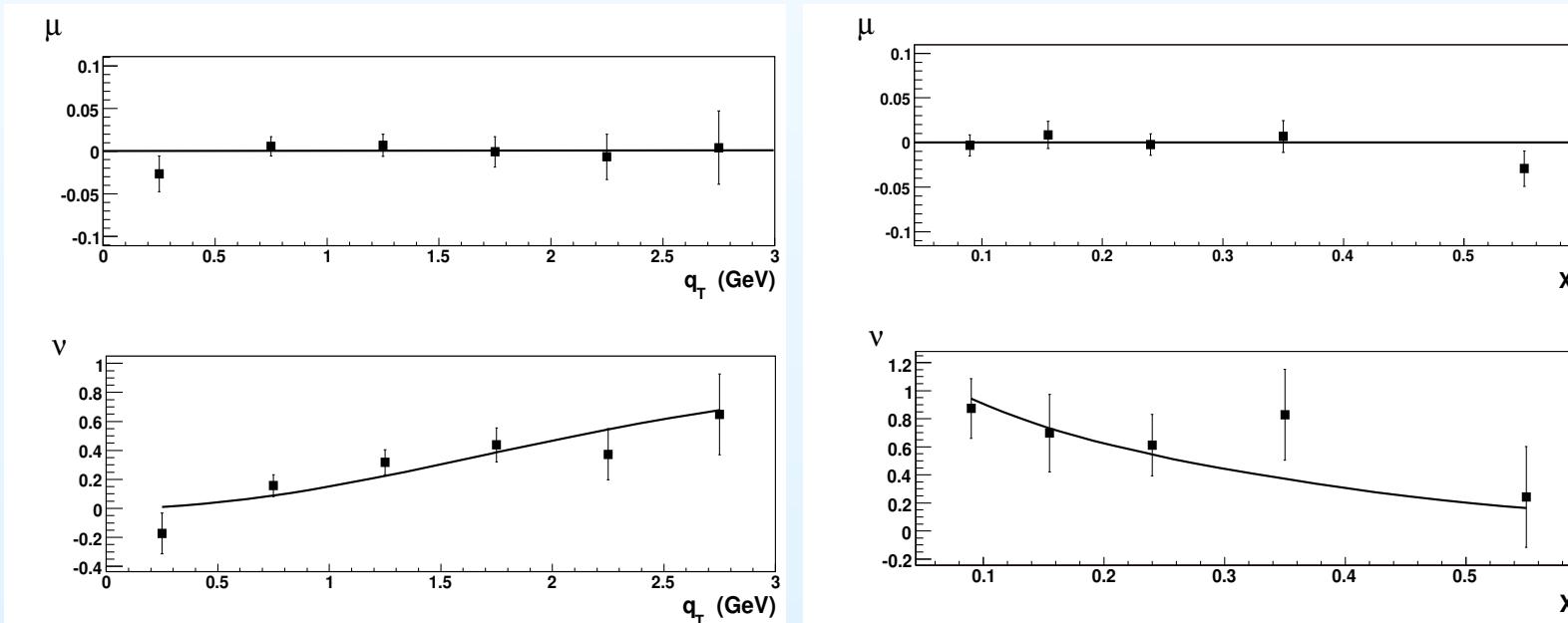
$$|h_{1u}| \leq (f_{1u} + g_{1u})/2$$

Collider mode		Fixed target mode	
$h_{1u(max)} \simeq 2.3$	$h_{1u(max)}^{\perp(1)} \simeq 1.2$	$h_{1u(max)} \simeq 1.5$	$h_{1u(max)}^{\perp(1)} \simeq 0.8$
$\hat{k}_{(max)} \simeq 1.2$	$ \hat{A}_h{}_{(max)} \simeq 0.14$	$\hat{k}_{(max)} \simeq 1.4$	$ \hat{A}_h{}_{(max)} \simeq 0.17$

Simulations (testing)

Experiments on unpolarized DY: J.S. Conway et al, PRD 71 (2005) 074014; NA10 Collaboration, Z. Phys. C 31 (1986) 513, Z. Phys. C 37 (1988) 545

$$R = \frac{3}{16\pi} (1 + \lambda \cos^2 \theta + \mu \sin 2\theta \cos \phi + k \sin^2 \theta \cos 2\phi),$$
$$(\lambda \simeq 1, \mu \simeq 0, k \equiv \nu/2)$$

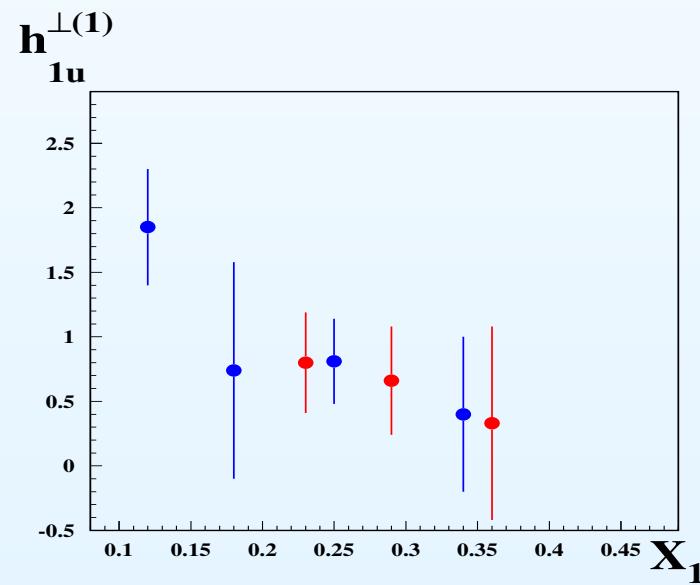
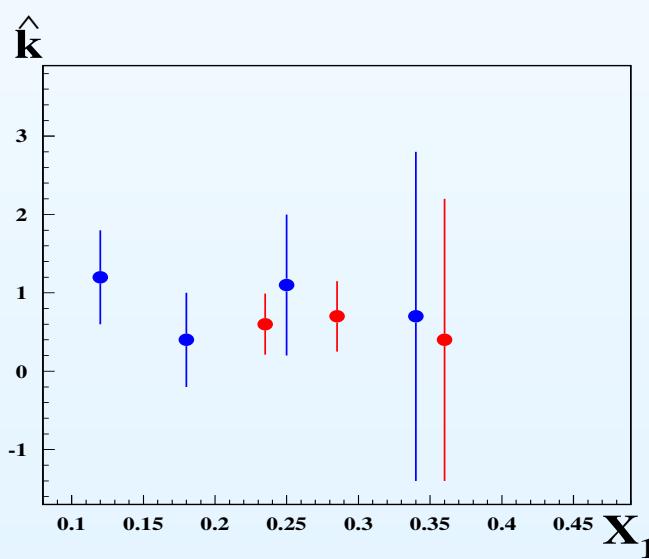


Simulations (results)

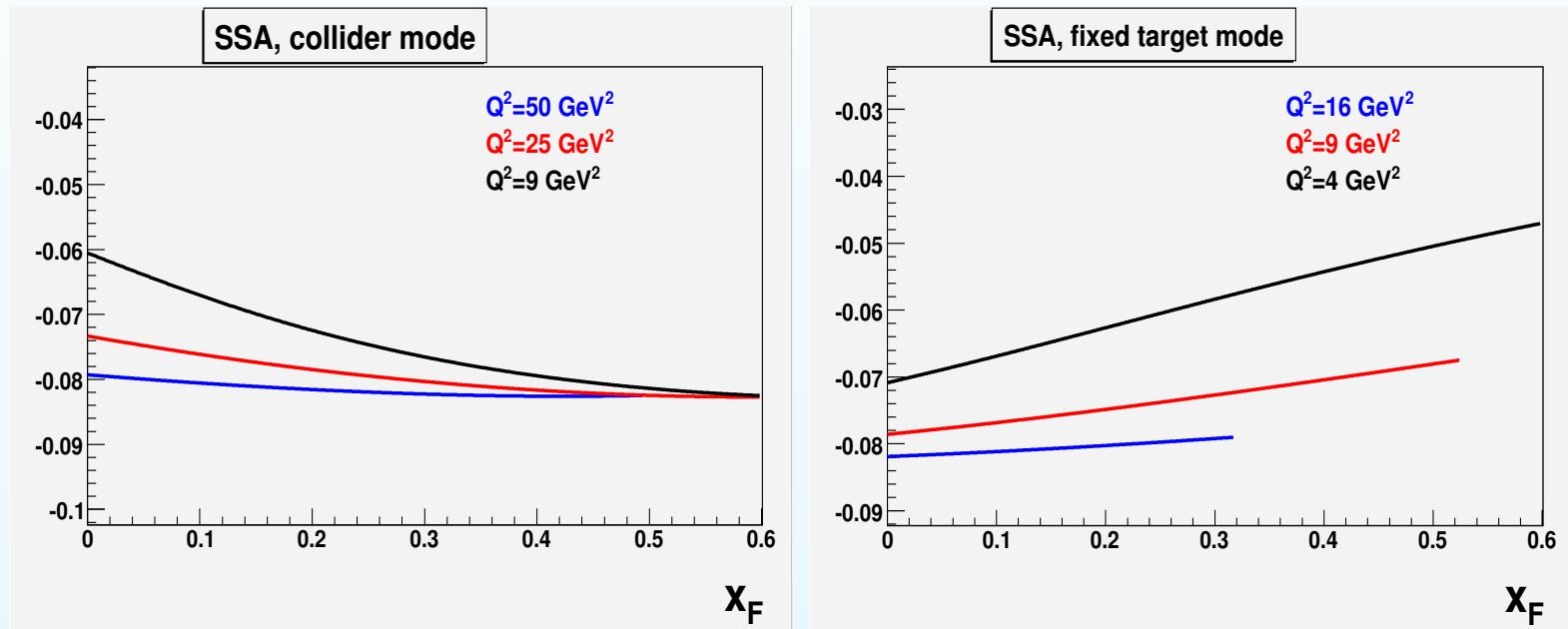
$$x \equiv x_1 \simeq x_2 \quad (x_F \simeq 0 \pm 0.4)$$

$$h_{1u}^{\perp(1)}(x) = f_{1u}(x) \sqrt{\frac{\hat{k}(x,x)}{8}}$$

$$h_{1u(x)} = -4\sqrt{2} \frac{\hat{A}_h(x,x)}{\sqrt{\hat{k}(x,x)}} f_{1u}(x)$$



Estimation of \hat{A}_h



Summary

- The procedure of direct (without any model assumptions) extraction of transversity and its accompanying T-odd PDF is proposed
- Both unpolarized and single-polarized DY processes necessary to extract the quantities h_1 and $h_1^{\perp(1)}$
- The preliminary estimations performed for PAX kinematics demonstrate that it is quite real to extract both h_1 and $h_1^{\perp(1)}$ in the PAX conditions.